#### MATH 1553, FALL 2018 SAMPLE MIDTERM 2: 3.5 THROUGH 4.4

Write your section number here:

Please read all instructions carefully before beginning.

- The maximum score on this exam is 50 points.
- You have 50 minutes to complete this exam.
- There are no aids of any kind (calculators, notes, text, etc.) allowed.
- Please show your work unless instructed otherwise. A correct answer without appropriate work will receive little or no credit. If you cannot fit your work on the front side of the page, use the back side of the page as indicated.
- You may cite any theorem proved in class or in the sections we covered in the text.
- Good luck!

This is a practice exam. It is meant to be similar in format, length, and difficulty to the real exam. It is **not** meant as a comprehensive list of study problems. I recommend completing the practice exam in 50 minutes, without notes or distractions.

The exam is not designed to test material from the previous midterm on its own. However, knowledge of the material prior to section §3.5 is necessary for everything we do for the rest of the semester, so it is fair game for the exam as it applies to §§3.5 through 4.4.

# Problem 1.

These problems are true or false. Circle <b>T</b> if the statement is <i>always</i> true. Otherwise, answer <b>F</b> . You do not need to justify your answer.			
a)	Т	F	Suppose <i>A</i> is a matrix with more columns than rows. Then the matrix transformation $T(x) = Ax$ cannot be one-to-one.
b)	Т	F	If <i>A</i> is an $n \times n$ matrix and $Ax = 0$ has only the trivial solution, then the equation $Ax = b$ is consistent for every <i>b</i> in $\mathbb{R}^n$ .
c)	Т	F	If <i>A</i> and <i>B</i> are $3 \times 3$ matrices and the columns of <i>B</i> are linearly dependent, then the columns of <i>AB</i> are linearly dependent.
d)	Т	F	There are linear transformations $T : \mathbb{R}^4 \to \mathbb{R}^3$ and $U : \mathbb{R}^3 \to \mathbb{R}^4$ so that $T \circ U$ is onto.
e)	Т	F	$V = \left\{ \begin{pmatrix} x \\ y \\ z \\ w \end{pmatrix} \text{ in } \mathbf{R}^4 \mid x - y = 1 + w \right\} \text{ is a subspace of } \mathbf{R}^4.$

Extra space for scratch work on problem 1

### Problem 2.



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#### Problem 4.



## Problem 5.

Parts (a), (b), and (c) are unrelated. You do not need to show any work for parts (a) and (b). **a)** I. Is the set  $\left\{ \begin{pmatrix} 0 \\ 0 \end{pmatrix}, \begin{pmatrix} 1 \\ 4 \end{pmatrix} \right\}$  linearly independent? YES NO II. If *A* is a  $3 \times 3$  matrix, is it possible that Col(A) = Nul(A)? YES NO **b)** Give a specific example of a subspace of  $\mathbf{R}^3$  that contains  $\begin{pmatrix} 1 \\ -1 \\ 2 \end{pmatrix}$ . (You may express this subspace any way you like, as long as you are clear.) c) Write a  $2 \times 3$  matrix A and a  $3 \times 2$  matrix B so that AB is the standard matrix for the transformation of *clockwise* rotation by  $90^{\circ}$  in  $\mathbb{R}^2$ . Compute *AB* to demonstrate that your answer is correct.