## Math 1553 Worksheet §6.4, 6.5

- **1.** Answer yes, no, or maybe. Justify your answers. In each case, *A* is a matrix whose entries are real numbers.
  - a) If *A* is a 3 × 3 matrix with characteristic polynomial  $-\lambda(\lambda 5)^2$ , then the 5-eigenspace is 2-dimensional.

**b)** If *A* is an invertible  $2 \times 2$  matrix, then *A* is diagonalizable.

c) A  $3 \times 3$  matrix *A* can have a non-real complex eigenvalue with multiplicity 2.

**d)** Suppose *A* is a  $7 \times 7$  matrix with four distinct eigenvalues. If one eigenspace has dimension 2, while another eigenspace has dimension 3, then *A* must be diagonalizable.

**2.** 
$$A = \begin{pmatrix} 2 & 3 & 1 \\ 3 & 2 & 4 \\ 0 & 0 & -1 \end{pmatrix}$$
.

**a)** Find the eigenvalues of *A*, and find a basis for each eigenspace.

**b)** Is *A* diagonalizable? If your answer is yes, find a diagonal matrix *D* and an invertible matrix *C* so that  $A = CDC^{-1}$ . If your answer is no, justify why *A* is not diagonalizable.