## Supplemental problems: Chapter 6

- **1.** True or false. If the statement is always true, answer true. Otherwise, answer false. Justify your answer.
  - a) Suppose  $W = \operatorname{Span}\{w\}$  for some vector  $w \neq 0$ , and suppose v is a vector orthogonal to w. Then the orthogonal projection of v onto W is the zero vector.
  - **b)** Suppose W is a subspace of  $\mathbf{R}^n$  and x is a vector in  $\mathbf{R}^n$ . If x is not in W, then  $x x_W$  is not zero.
  - c) Suppose W is a subspace of  $\mathbb{R}^n$  and x is in both W and  $W^{\perp}$ . Then x = 0.
  - **d)** Suppose  $\hat{x}$  is a least squares solution to Ax = b. Then  $\hat{x}$  is the closest vector to b in the column space of A.
- **2.** Let  $W = \operatorname{Span}\{\nu_1, \nu_2\}$ , where  $\nu_1 = \begin{pmatrix} -1 \\ 2 \\ 1 \end{pmatrix}$  and  $\nu_2 = \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix}$ .
  - **a)** Find the closest point w in W to  $x = \begin{pmatrix} 0 \\ 14 \\ -4 \end{pmatrix}$ .
  - **b)** Find the distance from w to  $\begin{pmatrix} 0 \\ 14 \\ -4 \end{pmatrix}$ .
  - **c)** Find the standard matrix for the orthogonal projection onto Span $\{v_1\}$ .
  - **d)** Find the standard matrix for the orthogonal projection onto W.
- **3.** Find the least-squares line y = Mx + B that approximates the data points (-2, -11), (0, -2), (4, 2).