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**I:** Consider the system of equations

$$x + 2y + uz = 1$$

$$-x + z = v$$

$$5x + 6y + 7z = 1$$

For which values of  $u$  and  $v$  does this system have a) no solution, b) exactly one solution, c) infinitely many solutions? Find the solution in case b) and find all the solutions in case c).

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**II:** Let  $T : R^2 \rightarrow R^2$  be the linear transformation obtained by first performing a rotation of  $30^\circ$  and then performing a reflection about the  $x = y$  axis. Find the matrix associated with  $T$ .

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**III:** Are the following vectors linearly independent?

$$\vec{v}_1 = \begin{bmatrix} 1 \\ 2 \\ 1 \end{bmatrix}, \quad \vec{v}_2 = \begin{bmatrix} 3 \\ 2 \\ 4 \end{bmatrix}, \quad \vec{v}_3 = \begin{bmatrix} 3 \\ -2 \\ 5 \end{bmatrix}$$

If not, give all the possible linear combinations of the zero vector in terms of  $\vec{v}_1, \vec{v}_2, \vec{v}_3$ .

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**IV:** a) What defines a linear transformation?

b) Which of the following linear transformations  $T : R^3 \rightarrow R^3$  is linear:

$$T_1(\vec{x}) = A\vec{x} + \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}$$

where  $A$  is a  $3 \times 3$  matrix.

$$T_2(\vec{x}) = \begin{bmatrix} |x| + z \\ z + x \\ x \end{bmatrix}$$

$$T_3(\vec{x}) = \begin{bmatrix} x + z \\ y + x \\ x \end{bmatrix}$$

c) What is the matrix associated with the linear transformation

$$T(\vec{x}) = \vec{a} \times \vec{x}$$

where

$$\vec{a} = \begin{bmatrix} a \\ b \\ c \end{bmatrix}$$

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**V:** Consider the linear transformation  $T : R^3 \rightarrow R^3$  that has the property that

$$T(\vec{e}_1 + \vec{e}_2) = \begin{bmatrix} 1 \\ 2 \\ 1 \end{bmatrix}, \quad T(\vec{e}_2 + \vec{e}_3) = \begin{bmatrix} 3 \\ 0 \\ 1 \end{bmatrix}, \quad T(\vec{e}_2 - \vec{e}_3) = \begin{bmatrix} 0 \\ -6 \\ -2 \end{bmatrix}$$

Is this linear transformation onto?