1. Prepquiz 1

Problem 1: Consider the trajectories of two particles, the first moves according to

 $\vec{r}_1(t) = (-5t^2 + 50t)\vec{k} + t\vec{i}$

where t denotes time and the second moves according to

$$\vec{r}_2(t) = (-5t^2 + 50t)\vec{k} + t\vec{i} + 2\vec{i}$$

a) Is there a time where these two particles meet, if yes, when?

b) Do the two curves described by these two motions intersect and if yes, where?

Problem 2: A curve is given in terms of

$$\vec{r}(t) = \cos t\vec{i} + \sin t\vec{j} + e^t\vec{k} \,,$$

where $0 \le t \le 2\pi$. Compute the curvature of the curve at every point.

Problem 3: Sketch the quadrics given by the equations

a)
$$4x^{2} + \frac{y^{2}}{4} + z^{2} = 1$$
,
b) $4x^{2} - \frac{y^{2}}{4} + z^{2} = 1$,
c) $4x^{2} - \frac{y^{2}}{4} - z^{2} = 1$.

and

c)
$$4x^2 - \frac{y^2}{4} - z^2 = 1$$
.