

8.1.3

$$\frac{\partial u}{\partial t} = A g(x, t) + A \Delta x g(x + \Delta x, t) + A \Delta x p c$$

According to Newton's law of cooling, the rate of heat transfer is proportional to exposed area.

$$g = h(u - u(x, t))$$

$$A \Delta x g = C \Delta x h (u - u(x, t))$$

$$\frac{\partial^2 u}{\partial x^2} + \frac{kA}{hc} (u - u(x, t)) = \frac{K}{\rho c} \frac{\partial u}{\partial t}$$

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$$g(x) = Bx$$

$$Bn = \frac{a}{2} \int_0^a Bx \sin\left(\frac{n\pi x}{a}\right) dx$$

$$Bn = \frac{2P}{a} \int_0^a \left[-\cos\left(\frac{n\pi x}{a}\right) \right]$$

$$Bn = \frac{2Pa}{n\pi} \left[\cos\left(\frac{n\pi x}{a}\right) \right]_{x=0}^{x=a}$$

$$u(x, t) = \sum_{n=1}^{\infty} B_n \sin\left(\frac{n\pi x}{a}\right) \exp\left\{-\frac{n^2 \pi^2 k t}{a^2}\right\}$$