Math 1553 Worksheet $\S 5.3$ (and some more practice with §5.2)

1. Answer yes / no / maybe. In each case, $A$ is a matrix whose entries are real.
a) If $A$ is a $3 \times 3$ matrix with characteristic polynomial $-\lambda(\lambda-5)^{2}$, then the 5eigenspace is 2 -dimensional.
b) If $A$ is an invertible $2 \times 2$ matrix, then $A$ is diagonalizable.
c) If $A$ and $B$ are $3 \times 3$ matrices and both have eigenvalues $-1,0,1$, then $A$ is similar to $B$.
d) Suppose $A$ is a $7 \times 7$ matrix with four distinct eigenvalues. If one eigenspace has dimension 2 , while another eigenspace has dimension 3 , then $A$ must be diagonalizable.
2. Consider the matrix

$$
A=-\frac{1}{5}\left(\begin{array}{ll}
8 & 3 \\
2 & 7
\end{array}\right)
$$

a) Find, draw, and label the eigenspaces of $A$.

b) Compute $A^{100}$.

