

1. Chapter 4:

- a. Solve the IVP:  $y'' + 6y' + 3y = 0$ ;  $y(0) = 1$   $y'(0) = 0$
- b. Solve the ODE using the method of undetermined coefficients:  
 $y'' - 2y' - 3y = -3te^{-t}$
- c. Solve the ODE using variation of parameters:  
 $y'' + 4y' + 4y = t^{-2}e^{-2t}$

2. Chapter 5:

- a. Solve the IVP using the method of Laplace Transforms:  
 $y'' - 2y' + 2y = \cos t$ ;  $y(0) = 1$ ,  $y'(0) = 0$

- b. Find the Laplace transform of:

$$f(t) = \begin{cases} t^2 & 0 \leq t < 2 \\ 2 & 2 \leq t < 6 \\ \cos t & 6 \leq t < 10 \\ 0 & \text{otherwise} \end{cases}$$

- c. Find the inverse Laplace transform:

$$F(s) = \frac{e^{-s} + e^{-2s} - e^{-3s} - e^{-4s}}{s}$$

- d. Find the inverse Laplace transform:

$$F(s) = \frac{se^{-s}}{s^2 - 2s + 10}$$